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First principles study of local electronic and magnetic properties in pure and electron-doped Nd₂CuO₄

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Abstract

The local electronic structure of Nd₂CuO₄ is determined from *ab initio* cluster calculations in the framework of density functional theory. Spin-polarized calculations with different multiplicities enable a detailed study of the charge and spin density distributions, using clusters that comprise up to 13 copper atoms in the CuO₂ plane. Electron doping is simulated by two different approaches and the resulting changes in the local charge distribution are studied in detail and compared to the corresponding changes in hole-doped La₂CuO₄. The electric field gradient (EFG) at the copper nucleus is investigated and good agreement is found with experimental values. In particular a careful study of the various contributions to the EFG exhibits that the drastic reduction of the main component of the EFG in the electron-doped material with respect to La₂CuO₄ is due to a reduction of the occupancy of the $3d_{3r^2-r^2}$ atomic orbital. Furthermore, the chemical shieldings at the copper nucleus are determined and are compared to results obtained from nuclear magnetic resonance (NMR) measurements. The magnetic hyperfine coupling constants are derived from the spin density distribution calculated for different spin multiplicities.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

Soon after high- T_c superconductivity was discovered [1, 2] in hole-doped La_{2-x}(Ba, Sr)_xCuO₄ and YBa₂Cu₃O_{7- δ} materials, it was found [3] that electron-doped Nd_{2-x}Ce_xCuO₄ also superconducts. All these substances contain CuO₂ planes separated by block layers containing rare-earth ions, and, moreover, the parent compounds are insulating and exhibit quasi two-dimensional antiferromagnetism. The generic phase diagrams of electron- and hole-doped

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cuprates, however, are somewhat different and are not totally symmetric with respect to hole or electron doping. This is not unexpected since there are quite significant structural differences. In La₂CuO₄, the copper is six-fold coordinated with oxygens, whereas in Nd₂CuO₄, the apical oxygens are missing. To gain insight into the mechanism(s) of high- T_c superconductivity, investigations on the origin of similarities and differences between hole- and electron-doped materials are very important.

In a simplistic ionic picture the valencies of the Cu and the O are the same in the insulating state of the parent compounds La_2CuO_4 and Nd_2CuO_4 . The former substance becomes metallic upon hole doping and it is assumed that the doped hole goes to the planar oxygen sites. On the other hand, in Nd₂CuO₄, the metallic state is achieved by electron doping and the doped electrons are assumed to reside on the copper sites.

Electronic structure calculations [4] in the framework of the full-potential linearized augmented-plane-wave method within the local density approximation have shown very similar band structures for Nd₂CuO₄ and La₂CuO₄. Details of the influence of electron or hole doping in these materials, however, cannot be obtained from band structure calculations except in the approximation of rigid bands. In contrast, cluster calculations are ideally suited for investigations of how the local electronic structure is influenced by doping. Using two different methods of simulating doping, we have previously shown [5] that simulations of hole doping in La₂CuO₄ provide insight into the changes in the population of various orbitals on the copper and oxygen atoms. Both methods yielded on the whole the same results and the changes calculated for the electric field gradient (EFG) at the copper agreed with experiments. Parts of this work deal with an adaptation of these methods to the case of the electron-doped cuprate Nd₂CuO₄.

A large body of data obtained by nuclear quadrupole resonance (NQR) and nuclear magnetic resonance (NMR) gives detailed information on the changes of the EFG values in all high- T_c superconductors. Several NMR experiments have been performed in the electron-doped Nd₂CuO₄ compound [6–11], the Pr_{1-x}LaCe_xCuO_{4- δ} material [12], the infinite layer compound [13–15] Sr_{1-x}La_xCuO₂, and its parent compound [16] SrCuO₂. The first surprising feature of these measurements is a relatively low ⁶³Cu NQR frequency (ν_Q) measured in the undoped parent compound compared to the hole doped compounds. In the undoped parent compound and 7.4 MHz in the infinite layer. This is less by more than a factor of two than in La₂CuO₄ (33.0 MHz [17]) and in YBa₂Cu₃O₇ (31.5 MHz [18]). The second striking feature of all NMR data on electron-doped cuprates is the extreme sensitivity of ν_Q to the doping level. Thus, ν_Q is ≤ 2 MHz for Nd_{1.85}Ce_{0.15}CuO₄ [10], ≤ 0.5 MHz in Pr_{0.91}LaCe_{0.09}CuO_{4- δ} [12] and finally ≤ 3 MHz in Sr_{0.9}La_{0.1}CuO₂ [14]. This strong doping dependence of the field gradient in the electron-doped compounds cannot be quantitatively explained [19] by simplistic ionic models [20].

In the present work we report on cluster calculations of the local electronic structure in Nd_2CuO_4 and its changes upon electron doping. The results are compared to those for holedoped La_2CuO_4 . The contributions to the EFG are studied in detail and it is explained why the EFG values in Nd_2CuO_4 are much smaller than in the hole-doped substances.

In section 2 we present the details of the technique of the cluster calculations. In section 3 the results for the electronic structure including the charge distribution, the EFG and their comparison to NMR experiments are given. In particular, in section 3.5, results for the chemical shieldings at the copper sites in undoped Nd_2CuO_4 are presented and are compared to results obtained from NMR experiments. The results for the spin density distribution and the calculation of magnetic hyperfine couplings are discussed in section 4. Section 5 contains a summary and conclusions.

Table 1. Compilation of the clusters used for Nd_2CuO_4 and some of their defining properties: number of atoms simulated by a full basis set (*N*), number of electrons (*E*) and number of basis functions (*B*).

Cluster	Ν	Ε	В
Cu ₅ O ₁₆ /Cu ₈ Nd ₂₄	21	295	403
Cu ₉ O ₂₄ /Cu ₁₂ Nd ₃₂	33	483	663
Cu ₁₃ O ₃₆ /Cu ₁₂ Nd ₄₈	49	711	975

2. The cluster method and computational details

2.1. General remarks

The idea of the cluster method is to solve the many-body Schrödinger equation for a portion of the crystal which we call the cluster. A cluster is a careful selection of a contiguous group of ions within a solid. The specific choice of the atoms that make up a cluster is such that it allows predominantly localized properties of a target atom and its vicinity to be calculated. A property is called *local* if it can be determined by the electronic structure of a few neighbouring atoms in the crystal. Electric field gradients (EFGs) and hyperfine fields are such local properties and have been successfully calculated by the cluster method (see for example [21, 22]). A cluster consists of three regions. The target atom and at least its nearest neighbouring atoms form the centre of the cluster and the corresponding electrons are treated most accurately using first-principles all-electron methods. This core region is embedded in a large cloud of a few thousand point charges at the respective lattice sites imitating the Madelung potential. Point charges at the border of the core region are replaced by basis-free pseudopotentials to improve the boundary conditions for the electrons in the cluster core. These pseudopotentials make up the so-called screening region.

It would be desirable to have clusters that contain as many atoms as possible in the core region but there are two computational limitations to the cluster size: the available computer resources and the convergence of the self-consistent field procedure. However, these limits have been pushed further since our first use of the cluster technique (see [23]), which now allows the computation of larger clusters and hence improves the bulk-to-surface ratio.

In this work three clusters of different size (with 5, 9, and 13 copper atoms in the core region) are studied and their constitutive properties are given in table 1. For clarity these clusters are labelled X/Y, where X is the chemical formula of the core region and Y the formula of the screening region.

2.2. Computational details

The atomic positions were chosen according to crystallographic structure determinations. The crystal structure of Nd₂CuO₄ is the so-called T' structure. A characteristic of this structure is the absence of apex oxygens in contrast to hole-doped materials. In this case the core region consists only of planar Cu and O. The lattice parameters (a = b = 3.95 Å and c = 12.07 Å) and the positions of the atoms within the unit cell have been adopted from references [25, 26]. The core region of the smallest cluster (Cu₅) for Nd₂CuO₄ incorporates 5 planar Cu atoms and their 16 nearest planar oxygen atoms. The screening shell includes bare pseudopotentials for 8 Cu²⁺ and 24 Nd³⁺ ions. The Madelung shell contains more than 6000 point charges. According to the attributed valences of copper and oxygen of 2⁺ and 2⁻, respectively, this cluster is given a total charge of 22⁻, leading to a total number of 295 electrons. We will also use Cu₉ and Cu₁₃ clusters, whose properties are given in table 1. The largest cluster (Cu₁₃) is schematically depicted in figure 1.



Figure 1. Schematic representation of the $Cu_{13}O_{36}/Nd_{48}Cu_{12}$ cluster. The 13 small black spheres denote the copper atoms simulated with basis sets, the 12 small grey (brown) spheres at the border of the cluster are the coppers represented by pseudopotentials.

For the atoms in the core region the standard 6-311G basis sets [24] were employed. The electronic structures in all the clusters described above were determined with the Gaussian03 quantum chemistry package [27] in the framework of density functional theory incorporating the exchange functional proposed by Becke [28], together with the correlation functional of Lee *et al* [29] (specified by the BLYP keyword in the Gaussian03 program).

Standard band theory calculations with the local density approximation (LDA) fail to describe the antiferromagnetic insulating state of the parent compounds of the cuprates [30]. Since the Cu d bands are not sufficiently localized [31], only upon introducing self-interaction corrections is the correct ground state obtained. In quantum-chemical approaches, however, one naturally uses a basis of localized orbitals. Performing the cluster calculations with different assumed spin configurations, one finds that in all cases (irrespective of the functional, LDA or generalized gradient approximation) the state with the lowest variational energy is found for the antiferromagnetic arrangement [22, 32].

The results of each calculation were examined with the Mulliken population analysis, which gives a description of the charge and spin densities in terms of the individual atoms and also the constituent orbitals. Other properties such as EFGs and hyperfine fields were also recorded at each copper centre. It is important to realize that properties calculated with the cluster method, such as for example EFGs or hyperfine fields, depend only marginally on the cluster size (see a detailed analysis in [33]).

2.3. Simulation of doping

There is an important aspect to consider when studying the change of the electronic structure upon doping cuprates by means of cluster calculations. If the doping is produced by impurity atoms (as for example replacing La^{3+} by Sr^{2+} in La_2CuO_4 or Nd^{3+} by Ce^{4+} in Nd_2CuO_4) one can investigate the local changes in the immediate neighbourhood of the impurity atoms. In this situation the doped charge carriers are 'pinned' around the dopant and are thus interpreted as *localized* holes (electrons). In contrast, we would like to investigate holes (electrons) *distributed* over the CuO₂ plane. Therefore we abstain from changing the chemical composition of our clusters but instead we simulate doping either (I) by simply removing (or adding) one electron or (II) by creating hole (electron) excess at the centre of the cluster by an additional electric field. Note that, in both methods, the nature of the dopant is not specified.

In this work we generalize the methods used in [5, 34] for the hole-doped material (La_2CuO_4) to the electron-doped material (Nd_2CuO_4) . If we simulate doping by adding an electron to the cluster (method I) the spin state of the cluster changes. The corresponding doping level is about 20% for a Cu₅ cluster, 10% for a Cu₉ cluster, and 8% for a Cu₁₃ cluster. It is therefore not possible to simulate an arbitrary doping level with this method.

For the second method we introduce additional point charges at the periphery of the cluster to create an electric field across the cluster in order to move the charge towards or away from the target atoms in the cluster centre. We call this method the *peripheral charge method*. Note that this added system of charges has no physical meaning. It is convenient because it can be continuously altered so that the charge can be progressively directed to or extracted from the target atoms in the centre of the cluster. This implies that the cluster must be sufficiently large so that ions of interest are not near the cluster edge. In contrast to the first method the cluster and the system of charges always have the same number of electrons and the same spin state, but the charge of the cluster can be progressively changed in a manner expected by doping. Of course this model has only a limited range of applicability and would ultimately break down for high doping levels since no electron is actually removed or added. The peripheral charge method serves to continuously interpolate the results already obtained with the first method (with remarkable success; see section 3.1).

3. Electronic structure

3.1. Charge distribution

In cluster calculations, the charge distribution is determined by the occupied molecular orbitals (MOs). The *m*th MO is represented as a linear combination

$$\phi_m(\vec{r}) = \sum_{K=1}^n \phi_m^K(\vec{r} - \vec{R}_K) = \sum_{K=1}^n \sum_{k=1}^{n_K} c_m^{K,k} B_{K,k}(\vec{r} - \vec{R}_K)$$
(1)

of n_K atomic basis functions $B_{K,k}$ centred at the nuclear sites K = 1, ..., n, and the $c_m^{K,k}$ are the MO coefficients². The charge density is then given by $\sum_m \phi_m(\vec{r})^2$ and contains both on-site and overlap terms. In the following we will use the Mulliken population analysis to describe the details of the charge distribution.

In the left part of figure 2 we have represented the partial Mulliken populations, p_c , for the relevant orbitals: $3d_{x^2-y^2}$, $3d_{3z^2-r^2}$, and 4s for Cu and $2p_{\sigma}$ for O_p . All other orbitals have populations that differ only marginally (<0.2%) from 2. Results have been obtained from calculations with clusters of three different sizes: Cu₅O₁₆/Cu₈Nd₂₄ with spin multiplicity M = 4, Cu₉O₂₄/Cu₁₂Nd₃₂ with M = 2, and Cu₁₃O₃₆/Cu₁₂Nd₄₈ with M = 6 for the undoped case. We find that the total energy is lowest for these multiplicities. They correspond to antiferromagnetic spin alignments. We repeated these calculations with one additional electron and, again, with a spin multiplicity leading to the lowest ground state energy (M = 3, 1, and 5 for Cu₅, Cu₉, and Cu₁₃, respectively). This doping simulation changes the total charge in the unit cell. We therefore define a quantity $\rho(3)$ as the sum of the Mulliken charge on the central copper atom and that on the adjacent oxygen atoms,

$$\rho(3) = \rho(Cu) + 2\rho(O_p) + 2, \tag{2}$$

which approximately represents the fractional excess charge in the unit cell. Ideally, in the undoped substance $\rho(3)$ should vanish. Due to open boundaries in the cluster method this is not quite exactly the case but since all calculated values are sufficiently close to zero we have renormalized the values for $\rho(3)$ such that they are indeed zero in the undoped compounds.

The full large grey (red) symbols are the partial Mulliken populations calculated in the Cu₅ cluster in the undoped case ($\rho(3) = 0$) and with one additional electron at $\rho(3) \approx -0.1$. The full small black (blue) symbols denote p_c values obtained from a cluster with 13 Cu, again in the undoped case and with an additional electron at $\rho(3) \approx -0.05$. The results of the calculation for the cluster with 9 atoms are not shown, although in the undoped case they are almost identical to those of Cu₁₃. However, when adding an electron, the results

² For the present discussion we do not need to distinguish the spin orbitals.



Figure 2. Partial Mulliken populations of the atomic orbitals versus doping level $\rho(3)$ for Nd_{2-x}Ce_xCuO₄ (left panel) and La_{2-x}Sr_xCuO₄ (right panel). The following orbitals are represented: $3d_{3z^2-r^2}$ (triangles down), 4s (circles), apical oxygen $2p_z$ (triangles up), $3d_{x^2-y^2}$ (diamonds) and the planar oxygen $2p_\sigma$ (squares). Open symbols refer to peripheral charge calculations and filled symbols refer to calculations where electrons are added or removed as appropriate (method I).

exhibit a peculiar superstructure for which at present we do not have a unique explanation. The open symbols, finally, represent partial populations that have been determined with the peripheral charge method described in section 2.3 that allows us to simulate the doping with fractional charges. These values have been obtained with the Cu₅ (Cu₁₃) cluster and result from calculations that all used the same spin multiplicity M = 4 (M = 6) as in the undoped case. (Note that the partial populations of the $3d_{3z^2-r^2}$, 4s, and $2p_{\sigma}$ orbitals in the Cu₅ and Cu₁₃ clusters for $\rho(3) = 0$ are so close that the corresponding markers nearly completely overlap.) It is seen that in the undoped case the partial populations only marginally depend on the cluster size. As a function of doping the p_c values calculated for the two differently sized clusters (filled symbols) change monotonically and are reasonably well interpolated by those obtained with the peripheral charge method (open symbols).

For a general discussion it is instructive to compare these results with those obtained previously by Stoll *et al* [5] for hole-doped $La_{2-x}Sr_xCuO_4$ which are shown in the right part of figure 2. Note that in this case $\rho(3)$ is defined by

$$\rho(3) = \rho(Cu) + 2\rho(O_p) + 2\rho(O_a) + 6.$$
(3)

Again, the full symbols denote partial Mulliken populations of the relevant atomic orbital (AO) calculated for the undoped material ($\rho(3) = 0$) for the cluster with 5 Cu atoms with M = 4 and with one electron less and M = 3 ($\rho(3) \approx 0.12$). The open symbols are obtained from calculations with the peripheral charge method.

By comparing the left and right sides of figure 2 it is first observed that there are no drastic differences between the electron-doped and hole-doped materials, although the latter have apical oxygens whose $2p_z$ orbitals are not completely filled. The populations of the Cu $3d_{x^2-y^2}$ orbitals (diamonds) and the O $2p_\sigma$ orbitals (squares) which carry most of the spin density slightly decrease from left to right. There is of course a discontinuity at $\rho(3) = 0$



Figure 3. Electron density difference contour plots in the x-z plane (perpendicular to the CuO₂ plane) between the Cu₁₃O₃₆/Cu₁₂Nd₄₈ and the Cu₁₃O₆₂/Cu₁₂La₇₄ clusters on a area of 4 $a_B \times 6 a_B$. The wave functions of the cluster electrons have been projected onto the 4s and the $3d_{3z^2-r^2}$ states. The solid density lines (black) occur when the local electron density of the cluster containing Nd is larger than the electron density of the cluster containing La. Dashed lines (red), on the other hand, denote that the local electron density is larger in the La-containing cluster. Two neighbouring lines (solid and dashed) are separated by an electron density difference of 0.01 e/a_B^3 .

which is due to the different structures (the lattice constant *a* for Nd₂CuO₄ is 4.8% larger than for La₂CuO₄).

It is remarkable that the Cu $3d_{3z^2-r^2}$ AO (triangles down) in the electron-doped material is less occupied than in La₂CuO₄. This is compensated by a significantly larger population of the Cu 4s AO (circles). In figure 3 the density difference in the 4s and $3d_{3z^2-r^2}$ AOs between the Cu₁₃O₃₆/Cu₁₂Nd₄₈ and Cu₁₃O₆₂/Cu₁₂La₇₄ is shown which demonstrates the increased population of the 4s at the expense of the $3d_{3z^2-r^2}$ AO.

3.2. Sensitivity of EFG values on charge distribution

A detailed description of the evaluation of EFGs in the framework of cluster calculations is found in [19]. Here we just point out the relevant aspects that are connected to the rearrangement of charge distributions due to electron doping.

We assume in the following that the target nucleus K_T is at $R_{K_T} = 0$. The contribution of the MO ϕ_m to the EFG at K_T is given by the matrix element

$$V_m^{ij} = \langle \phi_m(\vec{r}) | \frac{3x^i x^j - r^2 \delta^{ij}}{r^5} | \phi_m(\vec{r}) \rangle \tag{4}$$

$$=\sum_{K=1}^{n}\sum_{L=1}^{n}\sum_{k=1}^{n_{K}}\sum_{l=1}^{n_{L}}c_{m}^{K,k}c_{m}^{L,l}$$
(5)

$$\times \langle B_{K,k}(\vec{r} - \vec{R}_K) | \frac{3x^i x^j - r^2 \delta^{ij}}{r^5} | B_{L,l}(\vec{r} - \vec{R}_L) \rangle.$$
(6)

This matrix element contains contributions from basis functions centred at two nuclear sites, K

	- / ·		
		Undoped	e doped
		(M = 6)	(M = 5)
Ι	Reminder	0.755	0.797
	р	-1.431	-1.433
	$d_{x^2-v^2}$	-6.378	-6.613
	d _{xy}	-9.128	-9.088
	$d_{3z^2-r^2}$	8.309	8.222
	d_{xz}	4.528	4.512
	d _{yz}	4.528	4.512
II	S	-0.003	-0.002
	р	0.013	0.013
	$d_{x^2-y^2}$	-0.021	-0.020
	d _{xy}	0.001	0.001
	$d_{3z^2 - r^2}$	-0.585	-0.616
	d_{xz}	0.000	0.000
	d _{yz}	0.000	0.000
]	II + nuclei	-0.015	-0.017
Р	oint charges	-0.033	-0.033
	Total	0.538	0.234

Table 2. Contributions I, II, III to the EFG component V_{zz} in atomic units, calculated with DF/GGA for the NdCu₁₃ compound cluster, (undoped with spin multiplicity 6 and electron-doped with M = 5).

and L. Thus we can identify three types of contribution: (i) on-site terms from basis functions centred at the target nucleus ($K = L = K_T$, contribution I), (ii) mixed on-site and off-site contributions (II), and (iii) purely off-site terms with $K \neq K_T$ and $L \neq K_T$ (III).

In addition, there is a contribution coming from all nuclear point charges Z_K which we denote by W_{ij} . The charges of the bare nuclei at sites $K \neq K_T$ are screened by the matrix elements with K = L. Therefore the combined contributions from III and the nuclei (W_{ij}) are small. The partitioning of the contributions to the EFG tensor V_{ij} thus reads

$$V_{ij} = {}^{\mathrm{I}}V_{ij} + {}^{\mathrm{II}}V_{ij} + {}^{\mathrm{II}}V_{ij} + W_{ij}.$$
(7)

More details about these regional partitions can be found in [19].

We collect in table 2 the various contributions to V_{zz} at the copper obtained for the Cu₁₃O₃₆/Cu₁₂Nd₄₈ cluster for both the undoped and the electron-doped calculations. EFGs are given in atomic units (1 au corresponds to 9.717 × 10²¹ eV m⁻²). In the undoped case, the total value $V_{zz} = 0.538$ is obtained from contributions I (0.428), II (0.160), III + nuclei (-0.015) and a small correction due to the surrounding point charges (-0.033). In the electron-doped case the total EFG of $V_{zz} = 0.235$ is substantially smaller, which is mainly due to a diminished contribution from region I. Focusing on region I we note that the added contributions from the three AOs $3d_{xy}$, $3d_{zx}$, and $3d_{yz}$ are -0.072 (undoped) and -0.064 (doped).

A careful analysis of table 2 shows that the most significant difference is due to the $d_{x^2-y^2}$ and the $d_{3z^2-r^2}$ parts of contribution I. Only very small corrections are obtained by the other contributions. The influence of contribution III of the electrons on the other atoms is nearly fully compensated by the nuclear charges of these atoms and contributes only by a very small amount.

To understand the changes of the EFG on the copper sites upon doping, it is therefore sufficient to concentrate on the MOs which contain partially occupied $3d_{x^2-y^2}$ and $3d_{3z^2-r^2}$

Table 3. Partial occupation numbers *N*, partial Mulliken populations p_c , and expectation values $\langle r^{-3} \rangle$ for the relevant copper AOs in undoped (M = 6) and doped (M = 5) Cu₁₃ clusters representative of Nd₂CuO₄.

	Und	Undoped		Electron-doped		
	$3d_{x^2-y^2}$	$3d_{3z^2-r^2}$	$3d_{x^2-y^2}$	$3d_{3z^2-r^2}$		
Ν	1.379	1.820	1.435	1.806		
$p_{\rm c}$	1.430	1.865	1.483	1.856		
$\langle r^{-3} \rangle$	8.094	7.991	8.064	7.968		

AOs at the target nucleus. The EFG is then given by

$$V_{zz} = R + \frac{4}{7} (N_{3z^2 - r^2} \langle r^{-3} \rangle_{3z^2 - r^2} - N_{x^2 - y^2} \langle r^{-3} \rangle_{x^2 - y^2}), \tag{8}$$

where R is the contribution from all other orbitals and N are the partial occupation numbers of the corresponding orbitals which are gathered in table 3.

The fact that the partial occupation numbers *N* of the AOs are very similar to the partial Mulliken populations p_c which are also included in table 3 gives evidence that despite their simplistic concept the Mulliken charges can be significant quantities in the analysis of charge distributions in cuprates. In particular, the differences $N_{3z^2-r^2} - N_{x^2-y^2}$ and $p_c(3d_{3z^2-r^2}) - p_c(3d_{x^2-y^2})$ are very similar. In section 3.4 we will therefore use a simplified version of equation (8) for a more general analysis of the Cu EFGs in cuprates.

3.3. Comparison with experiments

The nuclear quadrupole frequency, v_0 , is related to the main component of the EFG, V_{zz} , by

$$\nu_{\rm Q} = \frac{3e}{2h} \frac{1}{I(2I-1)} Q V_{zz} \sqrt{1+\eta^2/3}.$$
(9)

Here, Q is the quadrupole moment of the nucleus under consideration and η is the anisotropy parameter. For I = 3/2 and for axial symmetry ($\eta = 0$) one has

$$\nu_{\rm Q} = \frac{e}{2h} Q V_{zz}.$$
 (10)

If we adopt the value of the quadrupole moment ${}^{63}Q = -0.211$ b derived by Sternheimer [20] we obtain from our calculations a quadrupolar frequency of ${}^{63}\nu_Q = 13.3$ MHz in the undoped Nd₂CuO₄, which is in very good agreement with the experimental value of $\nu_Q = 14$ MHz reported by Abe *et al* [7]. In the electron-doped materials we get ${}^{63}\nu_Q = 5.8$ MHz in the Cu₁₃ cluster (corresponding to a doping level of about 8%) and ${}^{63}\nu_Q = 3.6$ MHz in the Cu₅ cluster (corresponding to 20% doping). Experimental values for quadrupole frequencies in doped materials are generally much smaller than in the undoped case and close to zero ($\nu_Q < 2$ MHz in [10] for a doping level of 15%). This reduction compared to the undoped substance is at least qualitatively reproduced by our calculations.

3.4. General aspects of Cu EFG

It is often assumed (by making use of the simple ionic model) that the EFG can be used to give an estimate of the partial Mulliken population, $p_c(3d_{x^2-y^2})$, of the Cu $3d_{x^2-y^2}$ orbital. This is of course only true if one assumes that all the other d orbitals are fully occupied. If the population, $p_c(3d_{3z^2-r^2})$, of the Cu $3d_{3z^2-r^2}$ orbital is also less than 2, equation (8) must be used for the description of the EFG. If we replace the occupation numbers in equation (8) by the partial



Figure 4. Main component V_{zz} of the copper EFG in atomic units versus $\Delta_d = p_c(3d_{3z^2-r^2}) - p_c(3d_{x^2-y^2})$ for La₂CuO₄ (black square), YBa₂Cu₃O₇ (blue triangle up), YBa₂Cu₄O₈ (blue triangle down), YBa₂Cu₃O₆ (blue triangle right), Sr₂CuO₂Cl₂ (green circle), Nd₂CuO₄ (red diamond), Nd_{1,92}Ce_{0.08}CuO₄ (full red diamond).

Table 4. Partial Mulliken populations of the $3d_{x^2-y^2}$ and $3d_{3z^2-r^2}$ orbitals, their difference Δ_d , and the calculated EFG for La₂CuO₄, undoped and electron-doped Nd₂CuO₄, three substances of the YBaCuO family, and Sr₂CuO₂Cl₂ for Cu₁₃ clusters.

Mulliken populations					
Substance	$\overline{3d_{x^2-y^2}}$	$3d_{3z^2-r^2}$	4s	Δ_d	V_{zz}
La ₂ CuO ₄	1.406	1.922	0.502	0.516	1.186
Nd ₂ CuO ₄	1.430	1.865	0.647	0.435	0.574
Nd _{1.92} Ce _{0.08} CuO ₄	1.483	1.854	0.644	0.371	0.270
YBa2Cu3O7	1.423	1.914	0.590	0.492	1.047
YBa ₂ Cu ₄ O ₈	1.427	1.909	0.592	0.482	0.986
YBa2Cu3O6	1.428	1.902	0.618	0.474	0.807
$Sr_2CuO_2Cl_2$	1.450	1.899	0.525	0.450	0.718

Mulliken populations and if we assume that $\langle r^{-3} \rangle$ is similar for all 3d orbitals, we arrive at the following simplified formula:

$$V_{zz} \approx \frac{4}{7} \langle r^{-3} \rangle \Delta_d + R. \tag{11}$$

Here $\Delta_d = p_c(3d_{3z^2-r^2}) - p_c(3d_{x^2-y^2})$. In table 4 we have collected the relevant partial Mulliken populations $p_c(3d_{x^2-y^2})$ and $p_c(3d_{3z^2-r^2})$ together with Δ_d and V_{zz} for several cuprates (including YBa₂Cu₃O₆ [33], YBa₂Cu₃O₇ [22], YBa₂Cu₄O₈ [33], and Sr₂CuO₂Cl₂ [35]). For further reference table 4 also contains the 4s populations. In figure 4 we have plotted V_{zz} versus Δ_d for various cuprates. The linear correlation is evident and we thus conclude that the changes in V_{zz} depend almost entirely on the population of the $3d_{x^2-y^2}$ and the $3d_{3z^2-r^2}$ orbitals. This modification of the ionic model tells us that a small value of V_{zz} can also be obtained by an appropriate population difference of the $3d_{3z^2-r^2}$ and $3d_{x^2-y^2}$ AOs.

The relationship between the calculated and the *measured* EFGs will be discussed in depth in a subsequent paper [33].

3.5. Orbital shifts

For the cluster Cu_5O_{16}/Cu_8Nd_{24} we have also determined the chemical shielding tensor for the central copper nucleus in the same way as has been reported previously for La_2CuO_4

in [36]. The isotropic diamagnetic shielding is ${}^{63}\sigma_{dia} = 2400$ ppm. This value is, within a few ppm, the same for all Cu compounds. The paramagnetic shieldings are evaluated as ${}^{63}\sigma_{para}^{\parallel} = -(8000 \pm 800)$ ppm and ${}^{63}\sigma_{para}^{\perp} = -(2600 \pm 300)$ ppm for the field directions parallel and perpendicular to the *c*-axis, respectively. The error bars are estimated from the dependences of the size of the cluster. To compare these theoretical values with measurements we need to reassess the analysis of orbital shift measurements. As has been discussed in detail in [36], the NMR shifts for a nuclear species *k* are commonly determined as differences of frequencies measured in the same magnetic field in the target (*t*) substance and some reference (*r*) substance. Their connection with the chemical shieldings is given by

$${}^{k}K_{L}^{ii}(t-r) = {}^{k}\sigma_{dia}^{ii}(r) + {}^{k}\sigma_{para}^{ii}(r) - {}^{k}\sigma_{dia}^{ii}(t) - {}^{k}\sigma_{para}^{ii}(t).$$
(12)

For the copper nucleus, the reference substance is usually CuCl and in the above equation the diamagnetic terms cancel out:

$${}^{3}K_{L}^{\rm ii}(t - {\rm CuCl}) = {}^{63}\sigma_{\rm para}^{\rm ii}({\rm CuCl}) - {}^{63}\sigma_{\rm para}^{\rm ii}(t).$$
⁽¹³⁾

The paramagnetic shielding for CuCl, however, is substantial and has experimentally been determined by Lutz *et al* [37, 38] to be ${}^{63}\sigma^{iso}_{para}$ (CuCl) = -1500 ppm with an error of about 10 ppm. As it was done in [36] we introduce the notation of paramagnetic field modification ${}^{k}\overline{K}_{L}^{ii} = -{}^{k}\sigma^{ii}_{para}$. For copper in Nd₂CuO₄ we get

$${}^{63}\overline{K}_{L}^{\parallel} = (0.80 \pm 0.08)\%$$
 and ${}^{63}\overline{K}_{L}^{\perp} = (0.26 \pm 0.03)\%,$ (14)

which are similar to those calculated in [36] for YBa₂Cu₃O₇ (0.72% and 0.30%, respectively).

We are not aware of data for orbital shifts in doped Nd₂CuO₄. Detailed measurements, however, have been reported by Zheng *et al* [12] on Pr_{0.91}LaCe_{0.09}CuO_{4-y}. The deduced orbital shifts are ${}^{63}K_L^{\parallel} = 0.92\%$ and ${}^{63}K_L^{\perp} = 0.155\%$, measured relatively to the reference substance CuCl. After correction for ${}^{63}\sigma_{para}^{iso}$ (CuCl), as discussed above, one obtains the experimental paramagnetic field modifications ${}^{63}\overline{K}_L^{\parallel} = 1.07\%$ and ${}^{63}\overline{K}_L^{\perp} = 0.305\%$, respectively. Both values are considerably smaller than those reported from experiments in YBa₂Cu₃O₇ (1.43% and 0.43%). The agreement of the theoretical value for the perpendicular component with the experiment is reasonably good. The predicted value for ${}^{63}\overline{K}_L^{\parallel}$, however, is much smaller than that deduced from the data. The same discrepancy is also observed for hole-doped cuprates. We note, however, that the experimental value for ${}^{63}\overline{K}_L^{\parallel}$ is based on the observation of a temperature-independent total magnetic shift and the assumption that the on-site and transferred hyperfine fields cancel out in Pr_{0.91}LaCe_{0.09}CuO_{4-y}, as they do in the YBaCuO and LaSCO families. As will be discussed in section 4, our calculated values of the hyperfine couplings give no support for these incidental cancellations in substances with appreciable differences in the lattice parameters.

4. Spin density distribution and hyperfine couplings

6

The spin-polarized cluster calculations allow us to investigate the spin density distribution in detail. In figure 5(a) we depict the spin density distribution along the five Cu and six O obtained for the Cu₁₃O₃₆/Cu₁₂Nd₄₈ cluster with spin multiplicity M = 14, which corresponds to a ferromagnetic alignment of the copper moments represented in figure 5(b). Most of the spin density is provided by the singly occupied molecular orbital which is also highest in energy. It is a linear combination of $3d_{x^2-y^2}$ AOs on the coppers ($\approx 80\%$) and $2p_{\sigma}$ AOs on the oxygens ($\approx 20\%$). The square of the $3d_{x^2-y^2}$ AO has maxima at distances of 0.35 Å from the nucleus but vanishes at the nucleus. In general, the spin density at a nuclear site is due to s-type AOs



Figure 5. (a) Spin density along the five Cu and six O in the Cu₁₃O₃₆/Cu₁₂Nd₄₈ cluster of spin multiplicity M = 14; (c) spin density with multiplicity M = 6. (b) and (d) signs of the Mulliken spin densities.

giving rise to the Fermi contact term. In particular, the spin densities at the Cu nuclei (cusps in figure 5(a)) can be correlated with the Mulliken spin densities (whose signs are given in figure 5(b)) at the same and the nearest neighbour Cu nuclei. This observation can be used to split the Fermi contact term into on-site and transferred terms, as has been discussed in detail in [21, 22]. We just note here that the on-site term is negative if the Mulliken spin density at the Cu atom under consideration is positive and vice versa, and that the transferred term is positive (negative) if the Mulliken spin densities at the neighbouring Cu atoms is positive (negative). Near the oxygens, the spin density is provided by the $2p_{\sigma}$ AO and the small cusp at the position of the four innermost oxygen nuclei is due to the transferred hyperfine fields from the electronic moments of the two adjacent copper atoms. In figure 5(c) we show the spin density distribution obtained with spin multiplicity M = 6. For this multiplicity, the total energy is lower than for all other multiplicities and corresponds to an antiferromagnetic alignment of the copper moments represented in figure 5(d).

From the differences in the total energy of the various spin configurations it is possible to estimate the antiferromagnetic exchange interaction J, as will be described elsewhere [33]. Preliminary results indicate $J \approx 160$ meV for Nd₂CuO₄, which is about the same as in La₂CuO₄ and slightly larger than in YBa₂Cu₃O₇ ($J \approx 130$ meV).

The hyperfine coupling tensor at the copper is determined by an on-site term a_{tot}^{ii} and a transferred term b_{tot}^{ii} from the nearest neighbours. The value of a_{tot}^{ii} is made up of three contributions: an isotropic on-site interaction, a_{iso} , a dipolar interaction, a_{dip}^{ii} , and a contribution from spin–orbit coupling, a_{so}^{ii} . The transferred term, b_{tot}^{ii} , is dominated by the isotropic interaction, b_{iso} , since the dipolar term, b_{dip}^{ii} , is small and the influence of spin–orbit coupling is entirely neglected. In figure 6 we show the dependence of the isotropic hyperfine density, D_{iso} , at the Cu nucleus on the on-site atomic spin density, ρ_i , and those of the nearest neighbours, ρ_j . The straight line is a fit to the equation

$$D_{\rm iso} = a_{\rm iso} \cdot \rho_i + \sum_j b_{\rm iso} \cdot \rho_j \tag{15}$$

which allows the determination of a_{iso} and b_{iso} . Analogously, the dipolar contributions can be determined. The resulting hyperfine couplings are collected in table 5 and are compared



Figure 6. $D(Cu_i)/\rho(Cu_i)$ plotted against $\sum_{j \in NN} \rho(Cu_j)/\rho(Cu_i)$. Values for the cluster with multiplicity M = 14 (M = 6) are plotted with filled (open) symbols. The different markers correspond to symmetrically inequivalent copper sites in the cluster which differ for example by their number of nearest neighbours.

Table 5. Comparative table of the hyperfine constants for La_2CuO_4 and Nd_2CuO_4 (in units of a_B^{-3}).

	La_2CuO_4	Nd ₂ CuO ₄
a_{iso}	-1.94	-2.42
a_{dip}^{\parallel}	-3.55	-3.38
$b_{\rm iso}$	0.77	0.75
$b_{\mathrm{dip}}^{\parallel}$	0.08	0.03
$a_{\rm tot}^{\parallel}$	-3.30	-3.58
$a_{\rm tot}^{\perp}$	0.22	-0.34

to the values obtained for La₂CuO₄. The total values $a_{\text{tot}}^{\parallel}$ and a_{tot}^{\perp} include spin–orbit terms $a_{\text{so}}^{\parallel} = 2.222 a_{\text{B}}^{-3}$ and $a_{\text{so}}^{\perp} = 0.394 a_{\text{B}}^{-3}$ which have been estimated according to the procedure given in [21]. We note that the values for the two materials are very similar. The only significant change is in a_{tot}^{\perp} , which shows a different sign in the two substances.

From experiments there is much less information available for the hyperfine couplings in Nd₂CuO₄ than in the hole-doped materials. Zheng *et al* [12] reported spin shift measurements in $Pr_{2-x}Ce_xCuO_4$ and found, with the field parallel to the *c* axis, the same temperature-independent behaviour as has been observed in doped La₂CuO₄ and in the YBaCuO family. The spin shifts measured with field in the plane, however, change with decreasing temperature. This behaviour is commonly explained by a coincidental cancellation of the hyperfine coupling contributions in the *c*-direction. The theoretical values for $a_{tot}^{\parallel} + 4b_{tot}^{\parallel}$ are indeed close to zero. It is intriguing, however, that the same precise cancellation is required in most hole-doped materials and in $Pr_{2-x}Ce_xCuO_4$ to explain the temperature-independent spin shifts. More information on hyperfine couplings is available for the electron-doped infinite layer compound

SrCuO₂. There, $a_{tot}^{\perp} + 4b_{tot}^{\perp}$ should vanish to explain the data. Our calculated values give no support for these observations.

5. Summary and conclusions

Spin-polarized *ab initio* calculations have been performed to determine the local electronic structure of Nd₂CuO₄ using clusters comprising 5, 9, and 13 copper atoms in the CuO₂ plane. Electron doping has been simulated by two different approaches which both yield the same results. The local charge distribution has been discussed in detail in terms of the partial Mulliken populations of the individual atomic orbitals. The changes in the partial populations of the relevant AOs $(3d_{x^2-y^2}, 3d_{3z^2-r^2}, and 2p_{\sigma})$ that occur upon doping are relatively small but significant. Both $p_c(3d_{r^2-r^2})$ and $p_c(2p_{\sigma})$ slightly increase and $p_c(3d_{3r^2-r^2})$ is significantly less than 2. Electric field gradients depend sensitively on the non-spherical local charge distribution. The individual contributions to the EFG have been discussed in detail and the resulting value for the nuclear quadrupole frequency is in good agreement with the experiments. The comparatively small value and the changes upon doping have been explained by the differences in the occupation numbers $N_{x^2-y^2}$ and $N_{3z^2-r^2}$, which are close to the partial Mulliken populations p_c . The local electronic structure of Nd₂CuO₄ has been compared to that of La₂CuO₄. Hole doping in the latter material mainly decreases the population $p_c(3d_{x^2-y^2})$ and $p_{\rm c}(2p_{\sigma})$ but there is also a slight decrease of $p_{\rm c}(3d_{3z^2-r^2})$ and $p_{\rm c}(2p_z)$ of the apical oxygen. The different values in the EFG at the copper sites observed in the various cuprates can be understood by the difference in the partial Mulliken population $p_c(3d_{3r^2-r^2}) - p_c(3d_{x^2-y^2})$. The calculated spin density distribution in Nd₂CuO₄ is not much different from that determined for La_2CuO_4 and YBa₂CuO₇. The analysis of the magnetic hyperfine couplings, which is based on the dependence of the contact and dipolar spin densities, also yields values which are of similar magnitudes to those in hole-doped materials.

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